MAE 623 – Conduction Heat Transfer

Instructor: Dr. Terence Musho, PhD, PE Office: 727 ESB Phone: (304) 293-3256

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Office Hours: MW 11:00–12:00 PM (in person or Teams) **Lecture:** MWF 10:00–10:50 PM, ESB-441

Course Description

This course provides advanced knowledge and tools for solving complex conduction heat transfer problems. Emphasis is placed on analytical and approximate techniques, with extensions to microscale transport and numerical methods. Students will apply both theoretical and computational approaches to real-world conduction problems.

Texts and References

Primary Text: D. W. Hahn and M. N. Özışık, *Heat Conduction*, 3rd Ed., Wiley, 2012. Supplemental References:

- J.V. Beck, Heat Conduction using Green's Functions
- Z. Zhang, Nano/Microscale Heat Transfer
- M.N. Özişik, Inverse Heat Transfer: Fundamentals and Applications
- F.P. Incropera et al., Introduction to Heat Transfer

Course Objectives

- Derive and solve the heat equation in Cartesian, cylindrical, and spherical coordinates.
- Apply orthogonal functions, separation of variables, and integral transform techniques.
- Use Duhamel's theorem, Laplace transforms, and Green's functions for transient problems.
- Model conduction in composite media, phase-change systems, and moving heat sources.
- Evaluate the limits of Fourier's law at the microscale.
- Interpret solutions in the context of engineering systems and research.

Grading

Coursework Breakdown:

• Homework Assignments: 30%

• Midterm Exam: 30%

• Term Paper: 30%

• Participation/Activities: 10%

Policies

- Attendance is expected; participation in discussions is strongly encouraged.
- Homework is due on the posted date. Late work may be penalized unless arranged in advance.
- All submitted work must be original. Collaboration on homework is allowed only where specified.

- Exams are closed book unless otherwise stated. Academic integrity will be strictly enforced.
- Laptops/tablets are allowed for course-related activities only; phones must be silenced.
- Students requiring accommodations should notify the instructor early in the semester.

Tentative Course Schedule

Week	Lecture Topic	Reading (Hahn)	Assignment
1	Heat conduction fundamentals; Fourier's	Ch. 1.1–1.6	_
	law; heat equation; BCs and ICs		
2	Orthogonal functions; Sturm–Liouville;	Ch. 2	HW 1 Assigned
	Fourier series		
3	Separation of variables; 1D transient and	Ch. 3.1–3.4	_
	2D steady problems		
4	Semi-infinite/infinite domains; error	Ch. 6.1–6.3	HW 1 Due / HW 2 Assigned
	functions; similarity solutions		
5	Cylindrical problems; Bessel functions;	Ch. 4.1–4.3	_
	radial conduction		
6	Spherical problems; Legendre	Ch. 5.1–5.3	HW 2 Due / HW 3 Assigned
	polynomials; transient conduction		
7	Duhamel's theorem; time-dependent BCs	Ch. 7	—
	and sources		
8	Laplace transform method; transient	Ch. 9	HW 3 Due / HW 4 Assigned
	solutions		
9	Green's function approach; delta	Ch. 8.1–8.3	_
	functions; source representations		
10	Green's function applications;	Ch. 8.4–8.7	HW 4 Due / HW 5 Assigned
	Cartesian/cylindrical/spherical		
11	Composite media; multilayer slabs and	Ch. 10	_
	cylinders		
12	Moving heat sources; welding and	Ch. 11	HW 5 Due / HW 6 Assigned
	scanning analogies		
13	Phase change and Stefan problems;	Ch. 12	_
	enthalpy methods		
14	Approximate methods: integral method;	Ch. 13	HW 6 Due / HW 7 Assigned
	Galerkin approach	C) 11	
15	Integral transforms; Hankel and finite	Ch. 14	—
1.0	transforms; applications	01 17 10	
16	Anisotropy and microscale conduction;	Ch. 15, 16	HW 7 Due / HW 8 Assigned
1.5	limits of Fourier law		HIII a D
17	Term paper presentations; comprehensive		HW 8 Due
	review		